

# EdExcel Further Pure 1

## Complex Numbers

### Section 1: Introduction to complex numbers

#### Multiple Choice Test

1)  $(3 + 4i) - (2 - i) =$

- (a)  $1 + 3i$  (b)  $5 + 5i$   
(c)  $5 + 3i$  (d)  $1 + 5i$   
(e) I don't know

2)  $(2 + i)(3 - 2i) =$

- (a)  $8 + 5i$  (b)  $8 - i$   
(c)  $4 - i$  (d)  $4 + 5i$   
(e) I don't know

3)  $[(1 - 2i) + (1 + i)](-3 + i) =$

- (a)  $-7 + 5i$  (b)  $-7 - i$   
(c)  $-5 + 5i$  (d)  $5 - 5i$   
(e) I don't know

4) The roots of the equation

$$z^2 + 6z + 10 = 0$$

are

- (a)  $3 + i, 3 - i$  (b)  $3 + 2i, 3 - 2i$   
(c)  $-3 + 2i, -3 - 2i$  (d)  $-3 + i, -3 - i$   
(f) I don't know

5) Given that  $p + qi = \frac{1}{12 - 5i}$ , the values of  $p$  and  $q$  are given by

- (a)  $p = \frac{12}{169}, q = \frac{5}{169}$  (b)  $p = \frac{12}{169}, q = -\frac{5}{169}$   
(c)  $p = \frac{12}{119}, q = \frac{5}{119}$  (d)  $p = \frac{12}{119}, q = -\frac{5}{119}$   
(e) I don't know

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6) Which of the following complex numbers is not equal to the others?

(a)  $\frac{3+2i}{i}$

(b)  $\frac{13}{2+3i}$

(c)  $2-3i$

(d)  $\frac{13}{2-3i}$

(e) I don't know

7)  $z = \frac{3+4i}{2-3i}$ . The complex number  $w$  which satisfies the equation  $zw = 1$  is

(a)  $w = \frac{-6-17i}{5}$

(b)  $w = \frac{6+17i}{25}$

(c)  $w = \frac{-6-17i}{25}$

(d)  $w = \frac{6+17i}{5}$

(e) I don't know

8) The solution of the equation

$$(3-i)(z+4-2i) = 10+20i$$

is

(a)  $z = 46 - 52i$

(b)  $z = 1 - 3i$

(c)  $z = -3 + 9i$

(d)  $z = 5 + 5i$

(e) I don't know

9) Which of the following is NOT true?

(a)  $\frac{1}{i^3} - i = 0$

(b)  $\frac{1}{i} + i^3 = 0$

(c)  $i^4 = 1$

(d)  $\frac{1}{i^2} = i^2$

(e) I don't know

10) Which of the following statements is NOT true?

(a)  $z + z^*$  is real

(b)  $\frac{z}{z^*}$  is real

(c)  $zz^*$  is real

(d)  $z - z^*$  is pure imaginary

(e) I don't know

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## Solutions to Multiple Choice Test

1) The correct answer is (d)

$$\begin{aligned}3 + 4i - (2 - i) &= 3 + 4i - 2 + i \\ &= (3 - 2) + (4i + i) \\ &= 1 + 5i\end{aligned}$$

2) The correct answer is (b)

$$\begin{aligned}(2 + i)(3 - 2i) &= 6 - 4i + 3i - 2i^2 \\ &= 6 - i + 2 \\ &= 8 - i\end{aligned}$$

3) The correct answer is (c)

$$\begin{aligned}[(1 - 2i) + (1 + i)](-3 + i) &= (2 - i)(-3 + i) \\ &= -6 + 3i + 2i - i^2 \\ &= -6 + 5i + 1 \\ &= -5 + 5i\end{aligned}$$

4) The correct answer is (d)

$$\begin{aligned}z &= \frac{-6 \pm \sqrt{36 - 4 \times 1 \times 10}}{2} \\ &= \frac{-6 \pm \sqrt{-4}}{2} \\ &= \frac{-6 \pm 2i}{2} \\ &= -3 \pm i\end{aligned}$$

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5) The correct answer is (a)

$$\begin{aligned}p + qi &= \frac{1}{12 - 5i} \\&= \frac{12 + 5i}{(12 - 5i)(12 + 5i)} \\&= \frac{12 + 5i}{144 + 25} \\&= \frac{12}{169} + \frac{5}{169}i \\ \text{So } p &= \frac{12}{169}, \quad q = \frac{5}{169}.\end{aligned}$$

6) The correct answer is (d)

$$\begin{aligned}\frac{13}{2 - 3i} &= \frac{13(2 + 3i)}{(2 - 3i)(2 + 3i)} = \frac{26 + 39i}{13} = 2 + 3i \\ \frac{13}{2 + 3i} &= \frac{13(2 - 3i)}{(2 + 3i)(2 - 3i)} = \frac{26 - 39i}{13} = 2 - 3i \\ \frac{3 + 2i}{i} &= \frac{(3 + 2i)i}{-1} = \frac{3i - 2}{-1} = 2 - 3i \\ \text{So } \frac{13}{2 - 3i} &\text{ is not equal to the others.}\end{aligned}$$

7) The correct answer is (c)

$$\begin{aligned}w &= \frac{2 - 3i}{3 + 4i} \\&= \frac{(2 - 3i)(3 - 4i)}{(3 + 4i)(3 - 4i)} \\&= \frac{6 - 17i - 12}{25} \\&= \frac{-6 - 17i}{25}\end{aligned}$$

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8) The correct answer is (c)

$$(3-i)(z+4-2i) = 10+20i$$

$$\begin{aligned}z+4-2i &= \frac{10+20i}{3-i} \\ &= \frac{(10+20i)(3+i)}{(3-i)(3+i)} \\ &= \frac{30+70i-20}{10} \\ &= 1+7i \\ z &= 1+7i-4+2i \\ &= -3+9i\end{aligned}$$

9) The correct answer is (b)

$$i^4 = (i^2)^2 = (-1)^2 = 1$$

$$\frac{1}{i^3} - i = \frac{i}{i^4} - i = \frac{i}{1} - i = 0$$

$$\frac{1}{i^2} = \frac{i^2}{i^4} = \frac{i^2}{1} = i^2$$

$$\frac{1}{i} + i^3 = \frac{i^3}{i^4} + i^3 = \frac{i^3}{1} + i^3 = 2i^3 = -2i$$

10) The correct answer is (b)

$$\text{Let } z = x + iy, \text{ so } z^* = x - iy$$

$$z + z^* = x + iy + x - iy = 2x$$

$$z - z^* = x + iy - (x - iy) = 2iy$$

$$zz^* = (x + iy)(x - iy) = x^2 + y^2$$

so  $z + z^*$  is real

so  $z - z^*$  is pure imaginary

so  $zz^*$  is real

$$\frac{z}{z^*} = \frac{z^2}{zz^*} \quad zz^* \text{ is real but } z^2 \text{ is not, so } \frac{z}{z^*} \text{ is complex.}$$